The GCC Quad-Precision Math Library

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1 Typedef and constants

The following data type has been defined via typedef.

__complex128: __float128-based complex number

The following macros are defined, which give the numeric limits of the __float128 data type.

FLT128_MAX: largest finite number

FLT128_MIN: smallest positive number with full precision

FLT128_EPSILON: difference between 1 and the next larger representable number

FLT128_DENORM_MIN: smallest positive denormalized number FLT128_MANT_DIG: number of digits in the mantissa (bit precision) FLT128_MIN_EXP: maximal negative exponent FLT128_MAX_EXP: maximal positive exponent FLT128_DIG: number of decimal digits in the mantissa FLT128_MIN_10_EXP: maximal negative decimal exponent FLT128_MAX_10_EXP: maximal positive decimal exponent

The following mathematical constants of type **__float128** are defined.

M_Eq: the constant e (Euler's number) M_LOG2Eq: binary logarithm of 2 M_LOG10Eq: common, decimal logarithm of 2 M_LN10q: natural logarithm of 2 M_LN10q: natural logarithm of 10 M_PIq: pi M_PI_2q: pi divided by two M_PI_4q: pi divided by four M_1_PIq: one over pi M_2_PIq: one over two pi M_2_SQRTPIq: two over square root of pi

 M_SQRT2q : square root of 2

M_SQRT1_2q: one over square root of 2

2 Math Library Routines

The following mathematical functions are available:

acosq: arc cosine function acoshq: inverse hyperbolic cosine function asing: arc sine function asinhq: inverse hyperbolic sine function atanq: arc tangent function atanhq: inverse hyperbolic tangent function atan2q: arc tangent function cbrtq: cube root function ceilq: ceiling value function copysignq: copy sign of a number coshq: hyperbolic cosine function cosq: cosine function erfq: error function erfcq: complementary error function exp2q: base 2 exponential function expq: exponential function expm1q: exponential minus 1 function

fabsq: absolute value function fdimq: positive difference function finiteq: check finiteness of value floorq: floor value function fmaq: fused multiply and add fmaxq: determine maximum of two values fming: determine minimum of two values fmodq: remainder value function frexpq: extract mantissa and exponent hypotg: Eucledian distance function ilogbq: get exponent of the value isinfq: check for infinity isnang: check for not a number issignalingq: check for signaling not a number jOq: Bessel function of the first kind, first order j1q: Bessel function of the first kind, second order jng: Bessel function of the first kind, *n*-th order ldexpq: load exponent of the value lgammaq: logarithmic gamma function llrintq: round to nearest integer value llroundq: round to nearest integer value away from zero logbq: get exponent of the value logq: natural logarithm function log10q: base 10 logarithm function log1pq: compute natural logarithm of the value plus one log2q: base 2 logarithm function

lrintq: round to nearest integer value **lroundq**: round to nearest integer value away from zero modfq: decompose the floating-point number nanq: return quiet NaN nearbyintq: round to nearest integer nextafterq: next representable floating-point number powq: power function remainderq: remainder function remquoq: remainder and part of quotient rintq: round-to-nearest integral value roundq: round-to-nearest integral value, return __float128 scalblng: compute exponent using FLT_RADIX scalbnq: compute exponent using FLT_RADIX signbitq: return sign bit sincosq: calculate sine and cosine simultaneously sinhq: hyperbolic sine function sing: sine function sqrtq: square root function tanq: tangent function tanhq: hyperbolic tangent function tgammaq: true gamma function truncq: round to integer, towards zero y0q: Bessel function of the second kind, first order y1q: Bessel function of the second kind, second order yng: Bessel function of the second kind, *n*-th order cabsq complex absolute value function cargq: calculate the argument cimagq imaginary part of complex number crealq: real part of complex number cacoshg: complex arc hyperbolic cosine function cacosq: complex arc cosine function casinhq: complex arc hyperbolic sine function casing: complex arc sine function catanhq: complex arc hyperbolic tangent function catang: complex arc tangent function ccosq complex cosine function: ccoshq: complex hyperbolic cosine function cexpq: complex exponential function cexpiq: computes the exponential function of "i" times a real value

clogq: complex natural logarithm clog10q: complex base 10 logarithm conjq: complex conjugate function cpowq: complex power function cprojq: project into Riemann Sphere csinq: complex sine function csinhq: complex hyperbolic sine function csqrtq: complex square root ctanq: complex tangent function ctanhq: complex hyperbolic tangent function

3 I/O Library Routines

3.1 strtoflt128 — Convert from string

The function strtoflt128 converts a string into a __float128 number.

```
Syntax __float128 strtoflt128 (const char *s, char **sp)
```

Arguments:

 \mathbf{S}

input string

sp the address of the next character in the string

The argument *sp* contains, if not NULL, the address of the next character following the parts of the string, which have been read.

Example

```
#include <quadmath.h>
int main ()
{
   ___float128 r;
   r = strtoflt128 ("1.2345678", NULL);
   return 0;
}
```

3.2 quadmath_snprintf — Convert to string

The function quadmath_snprintf converts a __float128 floating-point number into a string. It is a specialized alternative to snprintf, where the format string is restricted to a single conversion specifier with Q modifier and conversion specifier e, E, f, F, g, G, a or A, with no extra characters before or after the conversion specifier. The %m\$ or *m\$ style must not be used in the format.

```
Syntax int quadmath_snprintf (char *s, size_t size, const char *format,
...)
```

Arguments:

	s size format	output string byte size of the string, including trailing NUL conversion specifier string	
Note	On some targets when supported by the C library hooks are installed for printf family of functions, so that printf ("%Qe", 1.2Q); etc. works too.		
Example	#includ	e <quadmath.h> e <stdlib.h> e <stdio.h></stdio.h></stdlib.h></quadmath.h>	

```
int main ()
{
    __float128 r;
    int prec = 20;
```

```
int width = 46;
  char buf[128];
  r = 2.0q;
  r = sqrtq (r);
  int n = quadmath_snprintf (buf, sizeof buf, "%+-#*.20Qe", width, r);
  if ((size_t) n < sizeof buf)</pre>
   printf ("%s\n", buf);
    /* Prints: +1.41421356237309504880e+00 */
  quadmath_snprintf (buf, sizeof buf, "%Qa", r);
  if ((size_t) n < sizeof buf)</pre>
   printf ("%s\n", buf);
    /* Prints: 0x1.6a09e667f3bcc908b2fb1366ea96p+0 */
 n = quadmath_snprintf (NULL, 0, "%+-#46.*Qe", prec, r);
  if (n > -1)
    {
      char *str = malloc (n + 1);
      if (str)
        {
          quadmath_snprintf (str, n + 1, "%+-#46.*Qe", prec, r);
          printf ("%s\n", str);
         /* Prints: +1.41421356237309504880e+00 */
        }
     free (str);
    }
 return 0;
}
```

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